

Simplify the following and write your answer in standard  $a + bi$  form.

1.  $\sqrt{-45}$

2.  $\frac{4-2i}{-2-5i}$

3.  $i^{35}$

Solve the following equations for the given variable. If there is more than one solution, separate them with commas.

4.  $3u^2 - 10u + 21 = 0$

5.  $x^2 - 10x + 10 = 0$   
(by completing the square)

Form:

○  $(x + \underline{\quad})^2 = \underline{\quad}$

○  $(x - \underline{\quad})^2 = \underline{\quad}$

Solution

$x = \underline{\quad}$

6.  $2x^2 - 3x + 6 = 0$

Determine all the solutions to the equations below. If there is more than one solution, separate them with commas.

7.  $x^4 + 6x^2 - 8 = 0$

8.  $3(2^{2x}) + (2^x) - 4 = 0$

9.  $\log_3(22x - 4) - \log_3(x + 1) = 2$

10.  $3^{x+1} = 2^{5x-6}$

11.  $3^{x^2-3x+1} = 3^{2x-5}$

12. Suppose  $R(x)$  is a polynomial of degree 13 whose coefficients are real numbers. Also, suppose that  $R(x)$  has the following zeros:  $7, -8, 5i, -2 - 4i$ .

a) Find another zero of  $R(x)$ .

b) What is the maximum number of real zeros that  $R(x)$  can have?

c) What is the maximum number of non-real zeros that  $R(x)$  can have?

d) If the leading coefficient of the polynomial was  $-3$ , what can the polynomial look like? Find a polynomial expression that has all the properties mentioned in parts a)-d)

13. Find all the solutions to the equation  $10x^6 - 11x^5 - 32x^4 + 56x^3 - 16x^2 - 13x + 6 = 0$ , if  $x = 1$  is a zero of multiplicity 3.

Solve the following problems. If there is no solution, please state so.

14. A rocket model is launched with an initial velocity of 235 ft/s. The rocket's height  $h$  (in feet ) after  $t$  seconds is given by the following.

$$h = 235t - 16t^2$$

Find all the values of  $t$  for which the rocket's height is 151 feet. Round your answers to the nearest hundredth. If there is more than one answer, use or to separate them.

12. A loan of \$50,000 is made at 2.5% interest, compounded annually. Assuming no repayment is made, after how many years will the amount due reach \$80,000 or more? (Use a calculator if necessary.) Write the smallest possible whole number answer.