

Due on Tuesday June 9, 2015

Code of Academic Honesty

The work on this exam represents my own. I am allowed to use class notes and lectures. I am not allowed to get help from any other human being (classmates, other teachers, tutors, spouses, children, other family members,....).

Signature _____ Date: _____

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|---------------|
| GRADE: _____% |
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- (a) Sketch the angle $-7\pi/4$ in standard position. (2 points)

(b) Find (if possible) the complement and supplement of $3\pi/4$. (2 points)

(c) Express the angle 150° in radian measure as a multiple of π . (2 points)

(d) The angle measure of 3 radian is _____ in degree. Round to three decimal place. (2 points)

(e) The angle measure of $85^\circ 18' 30''$ is _____ in decimal degree form. Round to three decimal place. (2 points)

2. Use the value of the trigonometric function $\sin t = \frac{4}{5}$ to evaluate the following functions. Assume t is an acute angle. (6 points)

(a) $\sin(\pi - t)$

(b) $\sin(\pi + t)$

(c) $\cos(t)$

3. Given $\sec \theta = -2$, $\tan \theta > 0$. Find the exact values of $\sin \theta$ and $\cot \theta$. (8 points)

a) $\sin \theta$

b) $\cot \theta$

4. Use the function values $\csc \theta = \frac{\sqrt{13}}{2}$, $\sec \theta = \frac{\sqrt{13}}{3}$, and trigonometric identities, to find the following. (12 points)

a) $\sin \theta$

c) $\tan \theta$

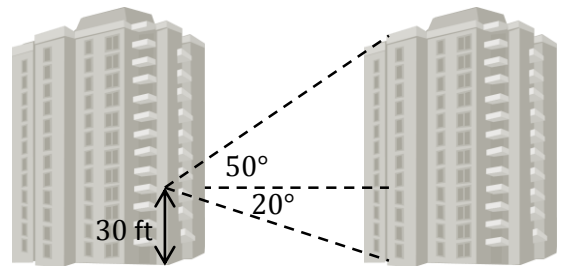
b) $\cos \theta$

d) $\sec(90^\circ - \theta)$

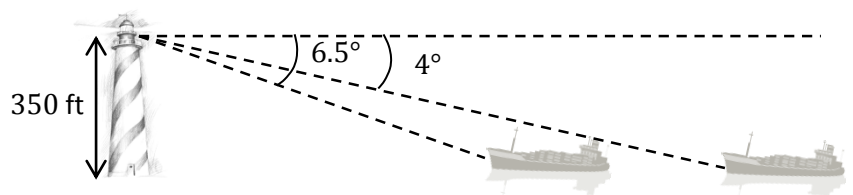
5. Evaluate the exact sine, cosine, and tangent of each angle without using a calculator. Show your work! (18 points)
- a) 225°
- b) -150°
- c) $\frac{10}{3}\pi$
6. Find two solutions of the equation $\tan \theta = -\sqrt{3}$. Give your answer in degrees ($0^\circ \leq \theta \leq 360^\circ$) and radians ($0 \leq \theta \leq 2\pi$). Do not use a calculator. (6 points)
7. If $\sin \theta = 0.3$, find the exact value of $\csc \theta + \cos\left(\frac{\pi}{2} - \theta\right)$. (4 points)
8. Find the acute angle θ that satisfies the equation $\tan \theta = \cot(\theta + 45^\circ)$. (4 points)

9. Show that the area A of an equilateral triangle is $A = \frac{\sqrt{3}}{4} a^2$, where a is the length of one of the three equal sides and θ is the measure of one of the three equal angles. (8 points)

10. From a window 30 ft above the street, the angle of elevation to the top of the building across the street is 50° and the angle of depression to the base of the building is 20° . Find the height of the building across the street. (8 points)



11. An observer in a lighthouse 350 feet above the sea level observes two ships directly offshore. The angles of depression are 4° and 6.5° . How far apart are the ships? (8 points)



12. The electromotive force E , in volts, in a certain ac circuit obeys the equation $E = 120 \sin (4\pi t - 10)$, $t \geq 0$.

(3 points)

a) What is the period?

b) What is the amplitude?

c) What is the phase shift?

13. Sketch the graph of the Trigonometric function $y = 3 \sin (x - \pi) - 2$. Include one full period. (5 points)