## Mat 110 Exam 3 Review

Name:

1. Find the solutions to the equations or inequalities below. All solutions must be exact solutions. Do not give an approximate solution. If there are extraneous solutions, please state so.
a. $3 x^{2}-11 x+10=0$
b. $3 x^{2 / 3}-11 x^{1 / 3}+10=0$
c. $\log _{2}(x-1)+3=\log _{2}(2 x+1)$
d. $3^{4 x-1}=5^{2+7 x}$
2. The number of bacteria in a certain population increases according to a continuous exponential growth model, with a growth rate parameter of $4.1 \%$ per hour. How many hours will it take for the sample to double?
3. The function below has at least one rational zero.
$h(x)=5 x^{4}-29 x^{3}-40 x^{2}-13 x-7$ Use this fact to find all zeros of the function.
a. Then write $h(x)$ as the product of irreducible factors.
b. Then sketch the graph of the function. Make sure you show all the $x$-intercepts and $y$-intercepts
c. Determine all the intervals where $h(x)<0$.
d. Find all solutions to $5 x^{4}-29 x^{3}-40 x^{2}-13 x-7=0$
e. Find all solutions to $5 x^{4}-29 x^{3}-40 x^{2}-13 x-7>0$
4. Caitlin invested $\$ 3200$ at $4.2 \%$ interest compounded quarterly. How many years will she will have to wait for double her money?
5. Solve the system of equations and inequalities below.
a. $\left\{\begin{array}{c}3 x+5 y \leq 1 \\ x-5 y>7\end{array}\right.$ (HINT: Graph the lines and shade the region that represents the solutions)
b. $\left\{\begin{array}{c}3 x^{2}+y^{2}=6 \\ 2 x^{2}-3 y^{2}=-7\end{array}\right.$
6. Create a system of equations that has the solutions $(2,1),(2,-1),(-2,1),(-2,-1)$.
